

DEPARTMENT OF MATHEMATICS  
UNIVERSITY OF MANITOBA

406

**FA/MATH 1020 Math In Art, Mid-Term Exam, 2006**

Examiners

Dr. R. Padmanabhan, Mathematics  
Professor David Lucas, School of Art

LAST NAME: (Print in ink) \_\_\_\_\_

FIRST NAME: (Print in ink) \_\_\_\_\_

STUDENT NUMBER: \_\_\_\_\_

FACULTY: School of Art      Science      University One

SIGNATURE: \_\_\_\_\_

(I understand that cheating is a serious offence)

Please show your work clearly.

Calculators are permitted.

Drawing instruments like ruler, compass, protractors  
are allowed.

Cell phones or other aids are not allowed.

The exam has a total of 6 pages (including this  
title page) and two blank sheets for rough work.  
Please check that you have all the pages.

There are 6 questions and each question carries 10  
points. The total value of all question is 60.

Please do not write  
in this column

1. \_\_\_\_\_/10

2. \_\_\_\_\_/10

3. \_\_\_\_\_/10

4. \_\_\_\_\_/10

5. \_\_\_\_\_/10

6. \_\_\_\_\_/10

Total \_\_\_\_\_/60

# FA/MATH 102- Mathematics in Art

## Mid-Term Test, 19 October, 2006

page 1 of 5  
time 70 minutes

1. In each of the following, numbers in the first column indicate the lengths of the three sides of a triangle. Determine the list of properties that are valid for the triangle in question.

triangle with sides a, b, c	equilateral triangle	isosceles triangle	golden triangle	right-angled triangle	no such triangle exists
5, 12, 13					
5, 5, 5					
5, 2, 2					
$1+\sqrt{5}$ , 2, 2					
3, 3, $\sqrt{18}$					

10

2. Divide the given segment AB (of length 12 cm) into seven equal parts by using ruler and compass. Measure the actual length  $12/7$  that you have obtained with a marked ruler. Also, obtain the value of  $12/7$  (i.e.  $12 \div 7$ ) using a calculator and compare the two values.

A ————— B

10

# FA/MATH 102- Mathematics in Art

## Mid-Term Test, 19 October, 2006

page 2 of 5  
time 70 minutes

---

3. If  $\square$  ABCD is a *golden rectangle* with the shorter side  $AB = 11$  cm, what is the approximate size of the longer side CD?  
Draw such a rectangle in the space given below and subdivide it into a square and a smaller golden rectangle. Iterate this process as much as you can (say, at least four times) .  
Using the technique (of drawing with circular arcs) we saw in the class, draw a smooth spiral within the golden rectangle ABCD.

10

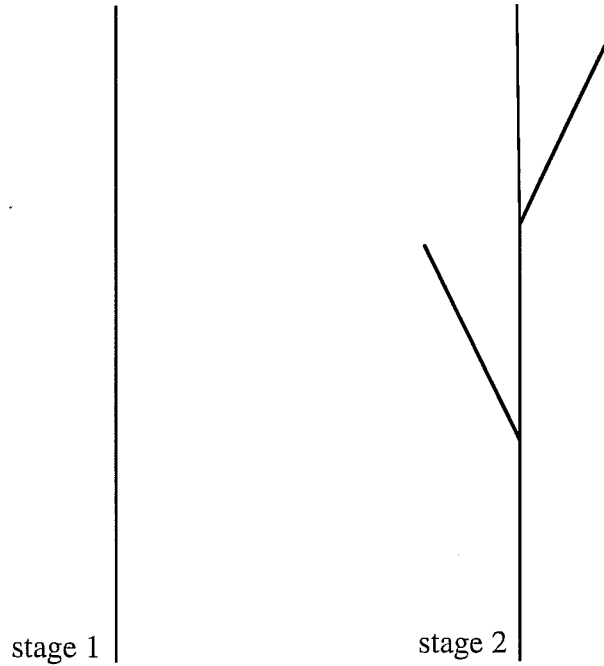
# FA/MATH 102- Mathematics in Art

## Mid-Term Test, 19 October, 2006

page 3 of 5  
time 70 minutes

4. Study the algorithm given by the first three stages of a fractal tree shown below and draw the next two stages of the fractal. Demonstrate self-similarity by circling a portion of your final sketch which is similar the entire tree in the previous stage.

10



# FA/MATH 102- Mathematics in Art

## Mid-Term Test, 19 October, 2006

page 4 of 5  
time 70 minutes

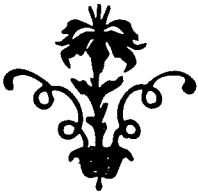

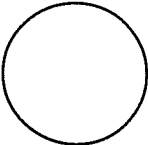
- 5 (a) Three points given below lie on a circle but unfortunately the circle itself got erased. Reconstruct the complete circle using the ruler and compass techniques. Locate the centre of the circle and determine the value of the radius of the circle.

4



- 5 (b). List the symmetries of each of the following designs. Use the notation  $\text{refl } \lambda$  (for mirror reflection about the line  $\lambda$ ),  $\text{rot}(C, \theta)$  (for rotational symmetry with centre  $C$  in degrees  $\theta$  counterclockwise. Mention the total number of symmetries for each of the designs

6

Design	symmetries	total number of symmetries
		
		
		

# FA/MATH 102- Mathematics in Art

## Mid-Term Test, 19 October, 2006

page 5 of 5  
time 70 minutes

---

6. You are commissioned to construct an obtuse golden triangle ABC using copper wire. If the total length of the wire is 7336 feet, what is the base BC of the largest golden triangle that you can construct?

