

THE UNIVERSITY OF MANITOBA

DATE: February 24, 2005

Midterm Examination

DEPARTMENT & COURSE NO. 136.130

TITLE PAGE

EXAMINATION: Vector Geometry & Linear Algebra

TIME: 1 Hour

EXAMINER: see below

NAME: (Print in ink) _____

STUDENT NUMBER: _____

SIGNATURE: (in ink) _____
(I understand that cheating is a serious offense)

Please indicate your instructor and section by placing
a check mark in the appropriate box below.

- | | | | |
|---|-----------------------------------|----------------------------|-------------|
| <input type="checkbox"/> Section <u>L05</u> | V. Charette | Tu, Th 10:00 am - 11:15 am | 208 Armes |
| <input type="checkbox"/> Section <u>L06</u> | N. Zorboska | M, W, F 1:30 pm- 2:20 pm | 204 Armes |
| <input type="checkbox"/> Section <u>L07</u> | K. Doerksen | M, W, F 1:30 pm- 2:20 pm | 223 Wallace |
| <input type="checkbox"/> Section <u>L08</u> | R.S.D. Thomas | M, W, F 2:30 pm- 3:20 pm | 208 Armes |
| <input type="checkbox"/> Section <u>L09</u> | J. Sichler | Tues. Evening | 204 Armes |
| <input type="checkbox"/> Section <u>L92</u> | Challenge for credit (SJR) | | |

INSTRUCTIONS TO STUDENTS:

This is a 1 hour exam. **Please show your work clearly.** Please justify your answers, unless otherwise stated.

No calculators or other aids are permitted.

This exam has a title page, 5 pages of questions and also 2 blank pages for rough work. Please check that you have all the pages.

The value of each question is indicated in the left-hand margin beside the statement of the question. The total value of all questions is 60.

Answer all questions on the exam paper in the space provide beneath the question. If you need more room, you may continue your work on the reverse side of the page, but **CLEARLY INDICATE** that your work is continued.

DO NOT WRITE IN
THIS COLUMN

1. _____ /12

2. _____ /6

3. _____ /9

4. _____ /4

5. _____ /7

6. _____ /11

7. _____ /11

TOTAL

_____ /60

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(12) 1. Solve the following system by Gauss-Jordan elimination:

$$3x_1 + 6x_2 \quad - 3x_4 = 0$$

$$2x_1 + 4x_2 + x_3 + x_4 = 0$$

$$x_1 + 2x_2 - x_3 + 4x_4 = 0$$

No marks will be given for any other method.

(6) 2. a) Find the determinant of $M = \begin{bmatrix} -2 & \sqrt{3} & 4 \\ 0 & 1 & 0 \\ 0 & 0 & 5 \end{bmatrix}$.

b) Suppose A is a 3×3 matrix that is **invertible**, and that it can be put into row-echelon form by the following sequence of elementary row operations:

- 1) add $\sqrt{2}$ times row 1 to row 2;
- 2) permute rows 2 and 3;
- 3) multiply row 3 by $\sqrt{5}$.

Find the determinant of A .

(9) 3. Let $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$. Express A^{-1} as an explicit product of elementary matrices.

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- (4) 4. Let A , B and C be $n \times n$ matrices and suppose that $2AB - 3AC = I_n$. Indicate how you can tell that A^{-1} exists, and find A^{-1} in terms of B and C .

- (7) 5. Let $X = [x_{ij}]$ be a 2×2 matrix. Given that $X + X^T = 0$ and $x_{12} = 7$, find X .

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(11) 6. Find the inverse of the following matrix by row reduction:

$$\begin{bmatrix} 2 & 0 & 1 \\ -2 & 1 & 0 \\ -2 & 0 & 1 \end{bmatrix}$$

No marks will be given for any other method.

(11) 7. Let $A = \begin{bmatrix} 2 & 2 & 0 \\ 2 & 0 & 2 \\ -2 & 2 & 2 \end{bmatrix}$. The adjoint of A is partially computed as shown. Enter the

two missing numbers in the boxes.

$$\text{Adj } A = \begin{bmatrix} -4 & -4 & \boxed{} \\ \boxed{} & -4 & -4 \\ 4 & -8 & -4 \end{bmatrix}.$$

Find $\det A$. Find A^{-1} .